

#### Science Standards:

Physical Science - Position and motion of objects Science and Technology - Abilities of technological design

Science and Technology - Understanding about science and technology

#### Science Process Skills:

Observing Measuring Collecting Data Interpreting Data

#### **Mathematics Standards:**

Mathematics as Communication Mathematics as Reasoning Mathematical Connections Estimation Number Sense and Numeration Geometry and Spatial Sense Measurement Trigonometry

#### Management:

Determining the altitude a rocket reaches in flight is a team activity. While one group of students prepares and launches a rocket, a second group measures the altitude the rocket reaches by estimating the angle of the rocket at its highest

point from the tracking station. The angle is

# **Teacher Information**

# Altitude Tracking

#### **Objective:**

To estimate the altitude a rocket achieves during flight.

#### **Description:**

In this activity, students construct simple altitude tracking devices for determining the altitude a rocket reaches in its flight.

then input into the altitude tracker calculator and the altitude is read. Roles are reversed so that everyone gets to launch and to track. Depending upon the number of launches held and whether or not every student makes their own Altitude

Trackers and Altitude Calculators, the activity should take about an hour or two. While waiting to launch rockets or track them, students can work on other projects.

Altitude tracking, as used in this activity, can be used with the *Paper Rockets* (page 61), *3-2-1 Pop!* (page 53), and *Bottle Rockets* (page 91) activities and with commercial model rockets. The Altitude Calculator is calibrated for 5, 15, and

# Materials and Tools:

- Altitude tracker pattern
- Altitude calculator pattern
- Thread or lightweight string
- Small washer
- Brass paper fastener
- Scissors
- Razor blade knife and cutting surface
- Stapler
- Meter stick
- Rocket and launcher



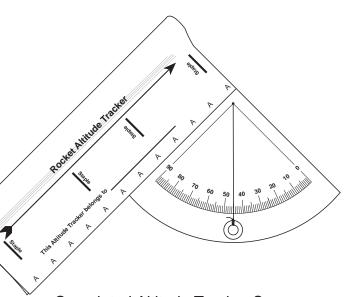
30 meter baselines. Use the 5-meter baseline for *Paper Rockets* and *3-2-1 Pop!* rockets. Use the 15-meter baseline for *Project X-35,* and use the 30-meter baseline for launching commercial model rockets.

For practical reasons, the Altitude Calculator is designed for angles in increments of 5 degrees. Younger children, may have difficulty in obtaining precise angle measurements with the Altitude Tracker. For simplicity's sake, round measurements off to the nearest 5 degree increment and read the altitude reached directly from the Altitude Calculator. If desired, you can determine altitudes for angles in between the increments by adding the altitudes above and below the angle and dividing by 2. A more precise method for determining altitudes appears later in the procedures.

A teacher aid or older student should cut out the three windows in in the Altitude Calculator. A sharp knife or razor and a cutting surface works best for cutting out windows. The altitude tracker is simple enough for everyone to make their own, but they can also be shared. ★Students should practice taking angle measurements and using the calculator on objects of known height such as a building or a flagpole before calculating rocket altitude.

#### **Background Information:**

This activity makes use of simple trigonometry to determine the altitude a rocket reaches in flight. The basic assumption of the activity is that the rocket travels straight up from the launch site. If the rocket flies away at an angle other than 90 degrees, the accuracy of the procedure diminishes. For example, if the rocket climbs over a tracking station, where the angle is measured, the altitude calculation will yield an answer higher than the actual altitude reached. On the other hand, if the rocket flies away from the station, the altitude measurement will be lower than the actual value. Tracking accuracy can be increased, by using more than one tracking station to measure the rocket's altitude. Position a second or third station in different directions from the first station. Averaging the altitude measurements will reduce individual error.





# Procedure:

#### Constructing the Altitude Tracker Scope

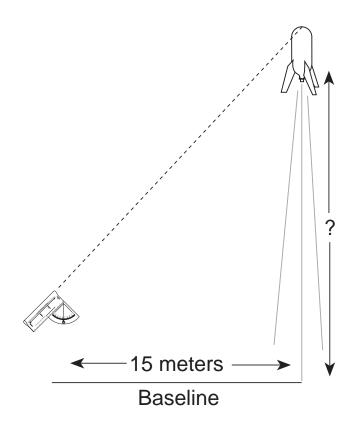
- 1. Copy the pattern for the altitude tracker on heavy weight paper.
- 2. Cut out the pattern on the dark outside lines.
- 3. Curl (do not fold) the B edge of the pattern to the back until it lines up with the A edge.
- 4. Staple the edges together where marked. If done correctly, the As and Bs will be on the outside of the tracker.
- 5. Punch a small hole through the apex of the protractor quadrant on the pattern.
- 6. Slip a thread or lightweight string through the hole. Knot the thread or string on the back side.
- 6. Complete the tracker by hanging a small washer from the other end of the thread as shown in the diagram above.

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## Procedure: Using the Altitude Tracker

 Set up a tracking station location a short distance away from the rocket launch site.
Depending upon the expected altitude of the



rocket, the tracking station should be 5, 15, or 30 meters away. (Generally, a 5meter distance is sufficient for paper rockets and antacid-power rockets. A 15-meter distance is sufficient for bottle rockets, and a 30-meter distance is sufficient for model rockets.

2. As a rocket launches, the person doing the tracking will follow the flight with the sighting tube on the tracker. The tracker should be held like a pistol and kept at the same level as the rocket when it is launched. Continue to aim the tracker at the highest point the rocket reached in the sky. Have a second student read the angle the thread or string makes with the quadrant protractor. Record the angle.

# Procedure:

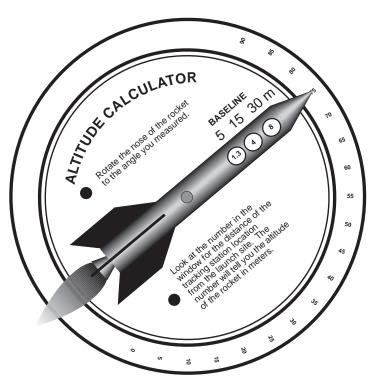
# **Constructing the Altitude Calculator**

- 1. Copy the two patterns for the altitude calculator onto heavy weight paper or glue the patterns on to light weight posterboard. Cut out the patterns.
- 2. Place the top pattern on a cutting surface and cut out the three windows.
- 3. Join the two patterns together where the center marks are located. Use a brass paper fastener to hold the pieces together. The pieces should rotate smoothly.

## **Procedure:**

#### **Determining the Altitude**

- Use the Altitude Calculator to determine the height the rocket reached. To do so, rotate the inner wheel of the calculator so that the nose of the rocket pointer is aimed at the angle measured in step 2 of the previous procedure.
- Read the altitude of the rocket by looking in the window. If you use a 5-meter baseline, the altitude the rocket reached will be in the window beneath the 5. To achieve a more accurate measure, add the height of the person holding the tracker to calculate altitude. If the angle falls between two degree marks, average the altitude numbers above and below the marks.





# Advanced Altitude Tracking:

- 1. A more advanced altitude tracking scope can be constructed by replacing the rolled sighting tube with a fat milkshake straw. Use white glue to attach the straw along the 90 degree line of the protractor.
- 2. Once you determine the angle of the rocket, use the following equation to calculate altitude of the rocket:

Altitude = tan∠x baseline

Use a calculator with trigonometry functions to solve the problem or refer to the tangent table on page 86. For example, if the measured angle is 28 degrees and the baseline is 15 meters, the altitude is 7.97 meters. *Altitude = tan* 28° X 15 m *Altitude =* 0.5317 x 15 m = 7.97 m

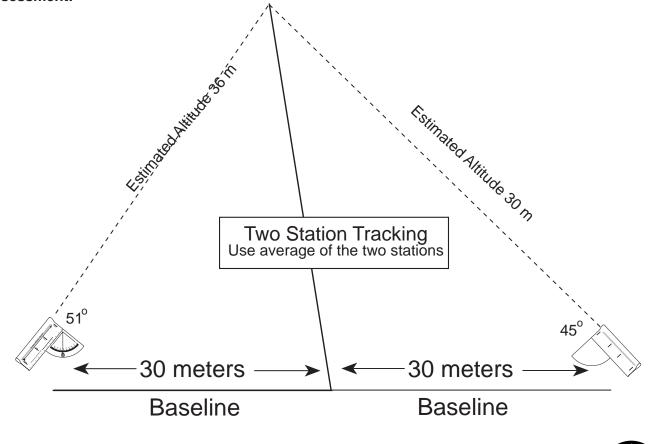
 An additional improvement in accuracy can be obtained by using two tracking stations. Averaging the calculated altitude from the two stations will achieve greater accuracy. See the figure below.

#### Assessment:

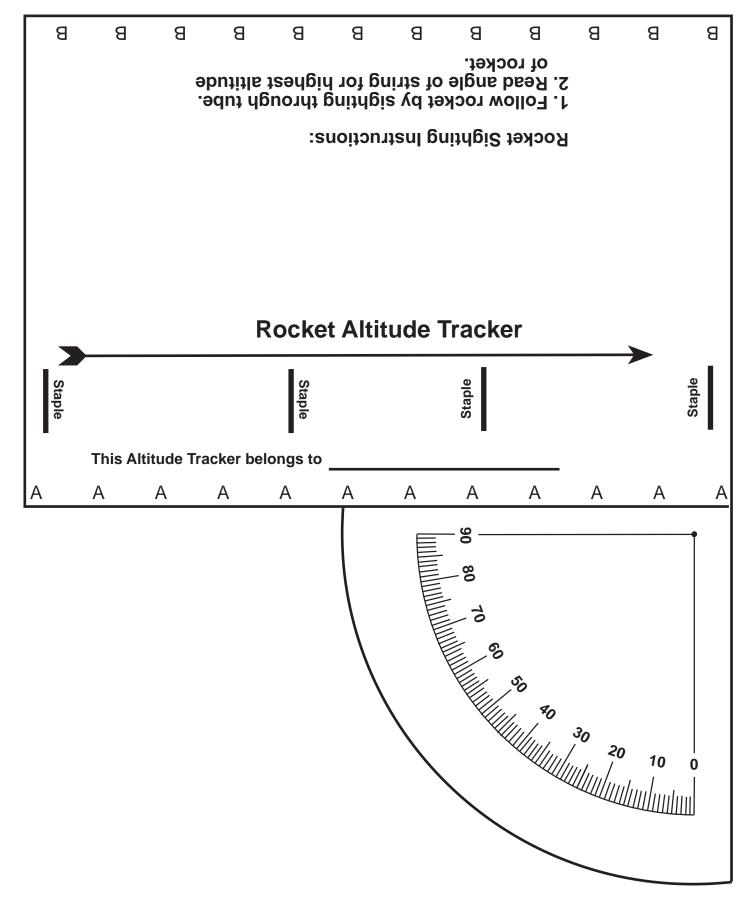
Have students demonstrate their proficiency with altitude tracking by sighting on a fixed object of known height and comparing their results. If employing two tracking stations, compare measurements from both stations. **Extensions:** 

#### Why should the height of the person holding the tracker be added to the measurement of the rocket's altitude?

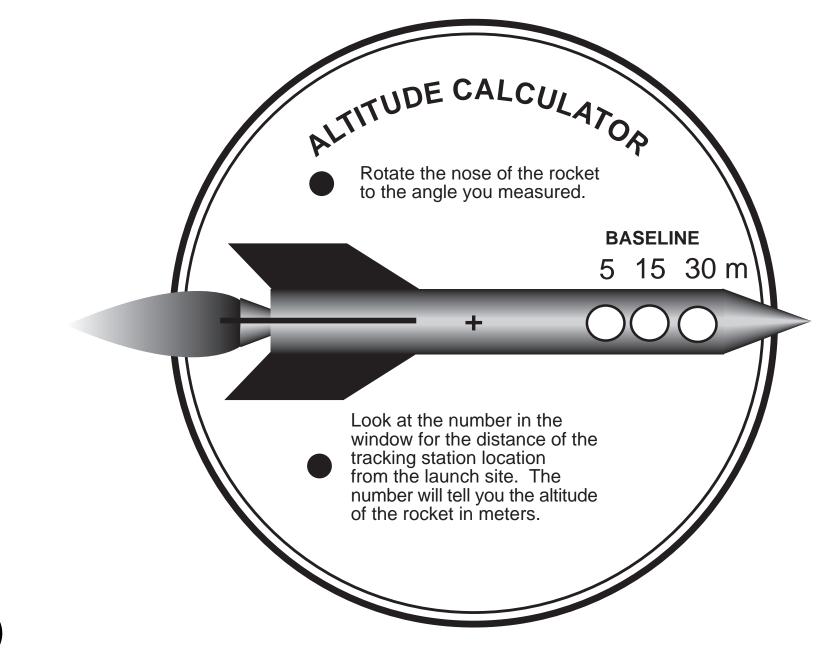
 Curriculum guides for model rocketry (available from model rocket supply companies) provide instructions for more sophisticated rocket trcking measurements. These activities involve two-station tracking with altitude and compass direction measurement and trigonometric functions.



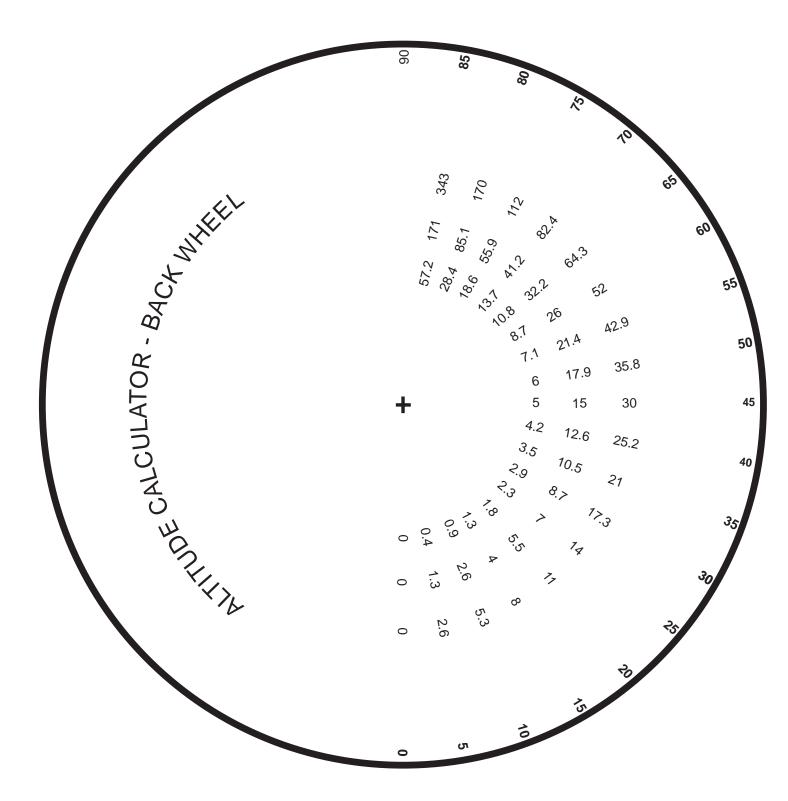














# **Tangent Table**

Degree	Tan	Degree	Tan	Degree	Tan
$\begin{array}{c} 0\\ 1\\ 2\\ 3\\ 4\\ 5\\ 6\\ 7\\ 8\\ 9\\ 10\\ 11\\ 12\\ 13\\ 14\\ 15\\ 16\\ 17\\ 18\\ 19\\ 20\\ 21\\ 22\\ 23\\ 24\\ 25\\ 26\\ 27\\ 28\\ 29\\ 30\\ \end{array}$	0.0000 0.0174 0.0349 0.0524 0.0699 0.0874 0.1051 0.1227 0.1405 0.1583 0.1763 0.2125 0.2308 0.2493 0.2679 0.2867 0.3057 0.3057 0.3249 0.3443 0.3639 0.3838 0.4040 0.4244 0.4452 0.4663 0.4877 0.5095 0.5317 0.5543 0.5773	$\begin{array}{c} 31\\ 32\\ 33\\ 34\\ 35\\ 36\\ 37\\ 38\\ 39\\ 40\\ 41\\ 42\\ 43\\ 44\\ 45\\ 46\\ 47\\ 48\\ 49\\ 50\\ 51\\ 52\\ 53\\ 54\\ 55\\ 56\\ 57\\ 58\\ 59\\ 60\\ \end{array}$	0.6008 0.6248 0.6494 0.6745 0.7002 0.7265 0.7535 0.7812 0.8097 0.8390 0.8692 0.9004 0.9325 0.9656 1.0000 1.0355 1.0723 1.1106 1.1503 1.1917 1.2348 1.2799 1.3270 1.3763 1.4281 1.4825 1.5398 1.6003 1.6642 1.7320	61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90	$\begin{array}{c} 1.8040\\ 1.8807\\ 1.9626\\ 2.0603\\ 2.1445\\ 2.2460\\ 2.3558\\ 2.4750\\ 2.6050\\ 2.7474\\ 2.9042\\ 3.0776\\ 3.2708\\ 3.4874\\ 3.7320\\ 4.0107\\ 4.3314\\ 4.7046\\ 5.1445\\ 5.6712\\ 6.3137\\ 7.1153\\ 8.1443\\ 9.5143\\ 11.4300\\ 14.3006\\ 19.0811\\ 28.6362\\ 57.2899\\\\ \end{array}$

